

Math



Algebra

1) Complete:-

- 1- $F(x) = X - 5$ its domain
- 2- If $F: R^+ \rightarrow R$, $F(x) = x^2$, then F is
[Even – odd – otherwise]
- 3- The domain $F: f(x) = \sqrt{-x}$ is
- 4- The range of the function $f(x) = |x+3| - 3$ is
- 5- The S.S of $|2x - 1| \leq 7$ in R is
- 6- The S.S of $|x-1| < 2$ in R is
- 7- The vertex of the curve $F(x) = 2 - (x+1)^2$
- 8- The domain of the function $F(x) = \frac{x}{\sqrt[3]{x-2}}$
- 9- The range of the function $F(x) = 5$ is
- 10- The domain of $f(x) = \sqrt{1-x}$ is
- 11- $F(x)$ is an even function then $\frac{f(a)+f(-a)}{f(a)} =$
- 12- The S.S of $|x| \leq 0$ is
- 13- The S.S of $|x-3| = 1$, then S.S
- 14- The range of $f(x) = (x+3)^2 - 3$ is
- 15 – The function $f(x) = |x|$ is increasing on
- 16- The equation of axis of symmetry of $f(x) = 5(x+2)^2 - 4$

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1) Graph each of the following functions then from the graph. Find the range and Monotonocity

2) Show whether it is even or odd.

a) $F(x) = x + |x|$

b) $F(x) = (x-2)^2 + 1$

c) $F(x) = x|x|$

d) $F(x) = |x-1|$

e) $F(x) = |x| + 1$

f) $f(x) = |x + 2|$

g) $F(x) = (x-3)^2$

h) $f(x) = x^2 + 4$

3) Find the S.S of the following :-

a- $|3x-4| < 5$

b- $|x-2| = 3x - 2$

c- $|2x+1| \leq 7$

d- $|x+2| \leq 0$

e- $|x+1| = 3x - 9$

f- $|3x - 2| = x$

4) Determine the type of each of the following functions:-

a- $F(x) = \sqrt{x^4 + x^2 - 5}$

b- $F(x) = \frac{x}{\cos x}$

c- $F(x) = \left(\frac{x^2}{3} - \frac{5}{x^4}\right)^5$

d- $F(x) = \frac{3x^2 - \cos x}{x^3 - 6x}$

e- $F(x) = \sin x^2 - \sin^2 x$

f- $F(x) = x \sin x^3$

5)

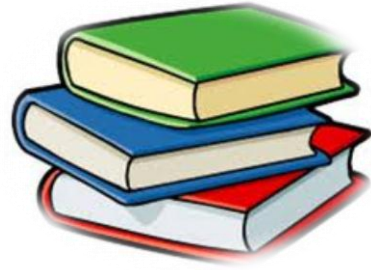
a- Graph the function:-

$$F(x) = \begin{cases} 2x & 0 \leq X < 2 \\ 8 - 2X & 2 < X \leq 4 \end{cases}$$

b- Find the range of the function then:

Deduce its monotoncity

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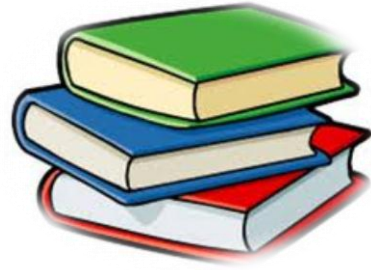


Answers Algebra

Complete:-

- 1- \mathbb{R}
- 2- Other wise
- 3- $]-\infty, 0]$
- 4- $[-3, \infty[$
- 5- $[-4, 4]$
- 6- $\mathbb{R} - [-1, 3]$
- 7- (-42)
- 8- $\mathbb{R} - \{8\}$
- 9- $\{5\}$
- 10- $]-\infty, 1]$
- 11- 2
- 12- $\{0\}$
- 13- $\{2, 4\}$
- 14- $(-3, -3)$
- 15- $[0, \infty[$
- 16- $X = -2$

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Calculus

1) Complete:-

$$1- \lim_{x \rightarrow 2} \frac{x^{-1} - 2^{-1}}{x^{-4} - 2^{-4}} = \dots\dots\dots$$

$$2- \lim_{x \rightarrow 2} \frac{3x+4}{\sqrt{2x} - 1} = \dots\dots\dots$$

$$3- \lim_{x \rightarrow 2} \frac{2x^3 - 16}{x - 2} = \dots\dots\dots$$

$$4- \lim_{x \rightarrow 2} \frac{2x^2 - 5x + 2}{x - 2} = \dots\dots\dots$$

$$5- \lim_{x \rightarrow 0} \frac{(x+2)^2 - 4}{x} = \dots\dots\dots$$

$$6- \lim_{x \rightarrow 1} \frac{x^8 - 1}{x^4 - 1} = \dots\dots\dots$$

$$7- \lim_{x \rightarrow 7} \frac{x^3 - 343}{x^2 - 49} = \dots\dots\dots$$

$$8- \lim_{x \rightarrow 3} \frac{x^2 - 1}{x - 3} = \dots\dots\dots$$

$$9- \lim_{x \rightarrow a} \frac{x^5 - a^5}{x - a} = \dots\dots\dots$$

$$10 - \lim_{x \rightarrow 0} \sqrt{4 - x^2} = \dots\dots\dots$$

$$11- \lim_{x \rightarrow -1} \frac{x^5 + 1}{x + 1} = \dots\dots\dots$$

$$12- \lim_{x \rightarrow 2} 10 = \dots\dots\dots$$

13- In any Triangle ABC: if $\frac{a}{\sin A} = 10$ then the radius of the circum circle of this triangle =cm.

14- In ΔXYZ , $2r \sin X = \dots\dots\dots$

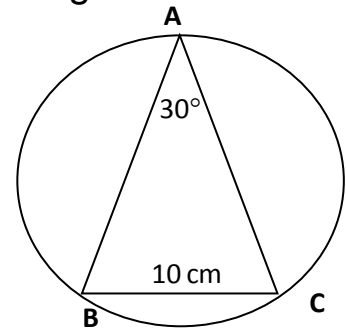
15- In ΔABC , If $m(\angle A) = 80^\circ$, $m(\angle B) = 60^\circ$, and $c = 12$ cm Then $a = \dots\dots$

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16- In $\triangle ABC$ $2 \sin A = 3 \sin B = 4 \sin C$ then $a : b : c = \dots\dots\dots$

17- In the opposite figure $BC = 10$ cm then the diameter length of the circle = $\dots\dots\dots$ cm.



18- An equilateral \triangle of side length 10 cm, then the length of the radius of its circum circle = $\dots\dots\dots$ cm.

19- In $\triangle ABC$, $(\angle B) = 30^\circ$ $b = \frac{5}{\pi}$ cm

The perimeter of circum circle = $\dots\dots\dots$ cm.

2) Find the result of of the following:-

1- $\lim_{x \rightarrow 1} \frac{x^2 + 6x - 7}{x^2 - 1}$

2- $\lim_{x \rightarrow 0} \frac{(x+2)^3 - 8}{3x}$

3- $\lim_{x \rightarrow 3} \frac{3x^2 - 27}{x^2 - x - 6}$

4- $\lim_{2x \rightarrow -1} \frac{32x^5 - 1}{64x^6 - 1}$

5- $\lim_{x \rightarrow -1} \frac{(2x+1)^2 - 1}{x - 1}$

6- $\lim_{x \rightarrow -2} \frac{2x^5 + 64}{x + 2}$

7- $\lim_{x \rightarrow 1} \frac{\sqrt{x+1} - 2}{x - 1}$

8- $\lim_{x \rightarrow 2} \frac{x^7 - 128}{x^2 + 3x - 10}$

9- $\lim_{x \rightarrow 2} \frac{2x^6 - 128}{x^2 - 4}$

10- $\lim_{x \rightarrow 5} \frac{x - 5}{\sqrt{3x+1} - 4}$

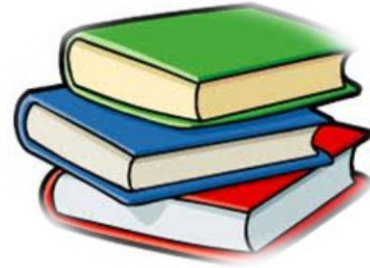
11- $\lim_{x \rightarrow -2} \frac{x^3 + 8}{x^5 + 32}$

12- In $\triangle ABC$ $a = 8$ cm, $b = 7$ cm and $m(\angle c) = 48^\circ$

I- The length of \overline{AB}

II- The radius length of the circum circle of $\triangle ABC$.

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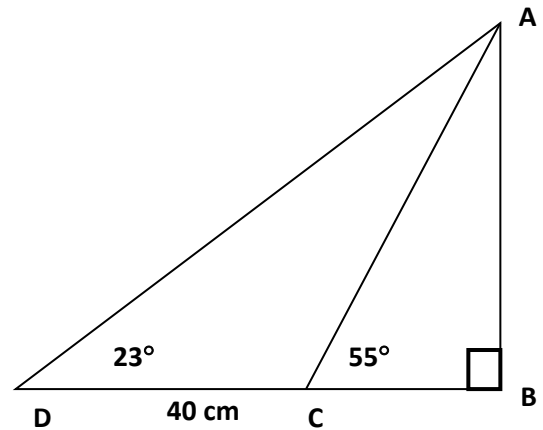
13- In $\triangle ABC$, if $a = 17.2$, $m(\angle B) = 47^\circ$, $m(\angle c) = 73^\circ$

Find the perimeter of the triangle.

14 – $m(\angle ADC) = 23^\circ$

$m(\angle ACB) = 55^\circ$ and $DC = 40\text{cm}$

Find the length of each of: \overline{AC} and \overline{AB}



3] Infinity

1) $\lim_{x \rightarrow \infty} \frac{3x^4 - x + 2}{5x^4 - 2}$

2) $\lim_{x \rightarrow \infty} \frac{2x^5 - x^3 + 2x}{7x^4 - 1}$

3) $\lim_{x \rightarrow \infty} \frac{x^2 + 3x + 2}{x^4 - 2}$

4) $\lim_{x \rightarrow \infty} \frac{(3x^4 - x)(x + 2)}{7x^5 - 2}$

5) $\lim_{x \rightarrow \infty} \frac{5x + 2}{\sqrt{x^2 - 2}}$

6) $\lim_{x \rightarrow \infty} \frac{\sqrt[4]{x^4 - x + 2}}{\sqrt[3]{8x^3 - 2}}$

7) $\lim_{x \rightarrow \infty} \frac{x\sqrt{x} + x - \sqrt{x^2 - 3}}{x + \sqrt{x^3 + 1}}$

8) $\lim_{x \rightarrow \infty} \frac{12^{\frac{1}{x}}}{x}$

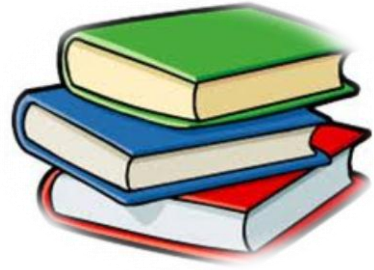
9) $\lim_{x \rightarrow \infty} \frac{3x^{-2} - x^{-3} + 2}{5x^{-2} + x^{-4} - 1}$

10) $\lim_{x \rightarrow \infty} \frac{2x^{-1} - x^{-2} + 2}{3x^{-1} - 7}$

11) $\lim_{x \rightarrow \infty} \frac{9^{\frac{1}{3}}}{x}$

12) $\lim_{x \rightarrow \infty} \frac{(3x^5 - 1)^2 (x^7 + 2)}{7(x - 3)^5 (x^2 - 2)^6}$

Math



Answers

1) Complete:-

1) $\frac{-1}{-4} \times 2^{-1+4} = 2$

2) 10

3) 24

4) 3

5) 4

6) 2

7) $\frac{21}{2}$

8) undefined

9) $5a^4$

10) 2

11) 5

12) 10

13) 5

14) χ

15) $\frac{12 \sin 80}{\sin 40}$

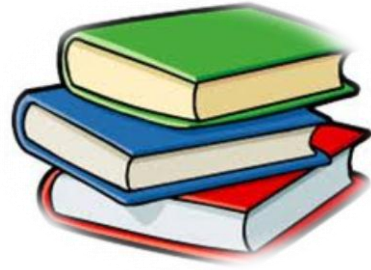
16) 6 : 4 : 3

17) diameter = 20cm

18) $\frac{10}{\sqrt{3}}$

19) 10cm

Math



2) Find the result of the following:

1) 4

2) 4

3) $\frac{18}{5}$

4) $\frac{-5}{6}$

5) 0

6) 80

7) The functions no limit $\left[\frac{\sqrt{2}-2}{0} \right]$

8) 64

9) 48

10) $\frac{8}{3}$

11) $\frac{3}{20}$

12) a) $C = 6.17$ cm.

b) $r = 4.15$ cm.

13) $b = 14.53$ cm.

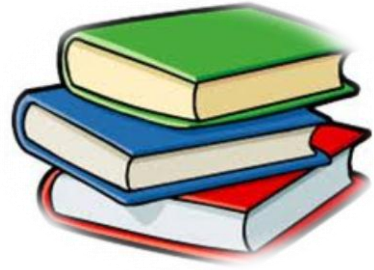
$c = 18.99$ cm.

per = 50.72 cm.

14) $AC = 29.49$ cm.

$AB = 24.16$ cm.

Math



3) Infinity

1) $(\frac{3}{5})$

2) (∞)

3) (0)

4) $(\frac{3}{7})$

5) 5

6) $(\frac{1}{2})$

7) 1

8) (0)

9) (-2)

10) $(\frac{2}{-7})$

11) (0)

12) $(\frac{3}{7})$

Math



Mechanics

- 1- Two forces are of magnitudes 5 and 10 newton act at a point and the measure of the included angle is 60° . Find the magnitude of their resultant and the measure of the angle which it makes with the first force.
($5\sqrt{7}$ newton , $40^\circ 53' 36''$)
- 2- Two force of magnitude 30 and 16N. act at a particle. If the magnitude of their resultant is 26 N. Find the measure of the angle between the forces.
(120°)
- 3- Find the magnitude and the direction of the resultant of two forces of magnitude 90 and 90 dyne if the measure of the included angle is 60°
($90\sqrt{3}$ dyne , $\theta = 30^\circ$)
- 4- Two forces 2 , F newton , the angle between them is of measure 120° . Find F in each of the following cases:
 - 1) The resultant = F
 - 2) The resultant perpendicular to the 2nd force.
 - 3) The resultant inclines by 45° to the 2nd force.
 - 4) The resultant bisects the angle between the forces.(2 , 1 , $\sqrt{3} + 1$, 2 newton)
- 5- Two concurrent force of magnitudes F_1 , F_2 N. , the magnitude of their resultant is R newton where $4 \leq R \leq 16$ and $F_1 > F_2$, Find:
 - 1)The magnitude of each of F_1 , F_2
 - 2)The magnitude of R if $\theta = 60^\circ$ ($F_1 = 10\text{N}$, $F_2 = 6\text{N}$. , $R = 14\text{N}$)

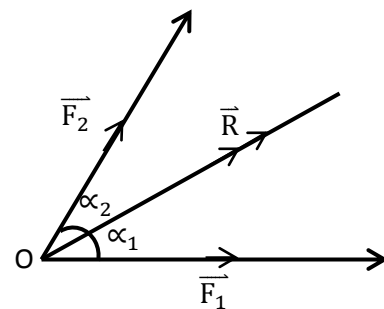
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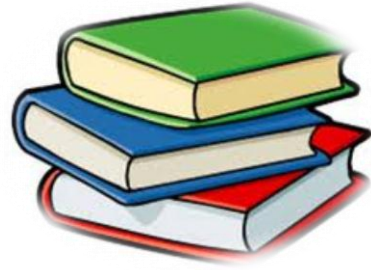
6- Five coplanar forces of magnitudes 7 , $4\sqrt{3}$, 8 , 6 and $9\sqrt{3}$ Kg. wt. act at a point in the directions of East , 30° North of East , 60° North of West of South and south respectively. Determine the magnitude and the direction of the resultant of these force. (12 kg. wt. , 60° South of East)

7- The forces 8 , $4\sqrt{3}$, $6\sqrt{3}$ and 14 newton act at a point , the measure of the angle between the first force and the second force is 30° , between the second and the third is 120° and between the third and the fourth is 90° . Find the magnitude and direction of the resultant of the resultant of these forces. (4 newton , 240°)

1) As resolving the force \vec{R} into two forces \vec{F}_1 and \vec{F}_2 making with \vec{R} two angles of measures α_1 and α_2 , then $F_1 = \frac{\dots}{\dots}$, $F_2 = \frac{\dots}{\dots}$



Math



Answers Mechanics

Solution:

1) $5\sqrt{7}$ newton , $40^\circ 53' 36''$

2) " 120° "

3) $90\sqrt{3}$ dune , $\theta = 30^\circ$

4) 2 , 1 , $\sqrt{3} + 1$, 2 Newton

5) $F_1 = 10N$, $F_2 = 6N$, $R = 14N$

6) 12Kg. wt. , 60° South of East

7) 4 Newton , 240°

8) $F_1 = \frac{\sin \alpha_2 \times R}{\sin (\alpha_1 + \alpha_2)}$, $F_2 = \frac{\sin \alpha_1 \times R}{\sin (\alpha_1 + \alpha_2)}$